

## FORMULAE IN PHYSICS STD. XII

### Chapter 1: Rotational Dynamics

(1) In uniform circular motion,

(a) Angular displacement ( $\theta$ ) =  $\frac{\text{Arc length (s)}}{\text{Radius (r)}}$

$$\text{i.e. } \theta = \frac{s}{r} \quad \text{or} \quad s = r\theta$$

(b) Angular speed ( $\omega$ ) =  $\frac{\theta}{t}$  or  $\vec{\omega} = \frac{d\theta}{dt}$

where  $\theta$  = angular displacement in time  $t$

(c) Angular acceleration ( $\alpha$ ) =  $\frac{\omega}{t}$  or  $\vec{\alpha} = \frac{d\vec{\omega}}{dt}$

(d) For one complete revolution  $\theta = 2\pi$  and  $t = T$

$$\therefore \omega = \frac{2\pi}{T} = 2\pi n$$

(e) Frequency =  $\frac{1}{\text{Period}}$  i.e....  $n = \frac{1}{T}$  or  $T = \frac{1}{n}$

(f) For one revolution,

$$\text{Period (T)} = \frac{2\pi r}{v} \quad \text{or} \quad T = \frac{2\pi}{\omega}$$

(2) Linear velocity = Radius  $\times$  angular velocity

$$v = r\omega$$

(3) The magnitude of the centripetal acceleration ( $a_c$ )

$$a_c = \frac{v^2}{r} = r\omega^2$$

(4) The magnitude of the centripetal force (F)

$$\text{C.P.F} = \frac{mv^2}{r} = mr\omega^2$$

(5) The magnitude of the centrifugal force (F)

$$\text{C.F.F.} = \frac{mv^2}{r} = mr\omega^2$$

(6) **Maximum and minimum speed:**

(a) Maximum speed of vehicle on plane horizontal road,

$$v_{\max} = \sqrt{\mu_s rg} \quad \text{where, } \mu_s = \text{coefficient of static friction.}$$

(b) For well of death minimum speed of vehicle,

$$\text{Minimum speed } (v_{\min}) = \sqrt{\frac{rg}{\mu_s}}$$

(c) For Banked road,

(i) Most safe speed ( $v_s$ ) =  $\sqrt{rg \tan \theta}$

(ii) Banking angle ( $\theta$ ) =  $\tan^{-1} \left( \frac{v^2}{rg} \right)$

(iii) Maximum speed of vehicle in terms of coefficient of friction for banked road,

$$v_{\max} = \sqrt{rg \left( \frac{\tan \theta + \mu_s}{1 - \mu_s \tan \theta} \right)}$$

(iv) Minimum possible speed in terms of  $\mu_s$  for banked road.

$$v_{\min} = \sqrt{rg \left( \frac{\tan \theta - \mu_s}{1 + \mu_s \tan \theta} \right)}$$

(7) **Conical pendulum:**

(a) The period of conical pendulum of length ( $l$ ) and semi vertical angle ( $\theta$ ) is

$$T = 2\pi \sqrt{\frac{l \cos \theta}{g}} \quad \text{or} \quad T = 2\pi \sqrt{\frac{r}{g \tan \theta}}$$

(b) Frequency of conical pendulum.

$$n = \frac{1}{2\pi} \sqrt{\frac{g}{l \cos \theta}} \quad \text{or} \quad n = \frac{1}{2\pi} \sqrt{\frac{g \tan \theta}{r}}$$

(c) If  $\theta$  is small  $\cos \theta \approx 1$ .  $\therefore$  Period (T) =  $2\pi\sqrt{\frac{l}{g}}$

**(8) For vertical circular motion:**

**Case-I:-** Mass tied to a string:-

(a) Difference in tension of lowest and highest point,

$$\therefore T_B - T_A = 6mg$$

(b) Velocity at highest point or top point (A)

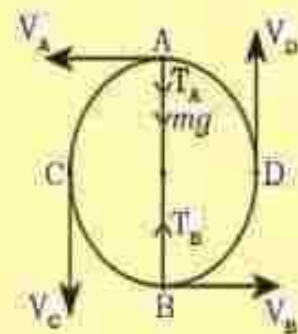
$$V_A = \sqrt{rg}$$

(c) Velocity at lowest point or Bottom (B)

$$V_B = \sqrt{5rg}$$

(d) Velocity at point C and D.

$$\therefore V_C = V_D = \sqrt{3rg}$$



**Case-II:-** Mass tied to a rod:-

(a) Difference in tension,  $T_B - T_A = 6mg$

(b) Velocity at top,  $V_A = 0$

(c) Velocity at bottom  $V_B = 2\sqrt{rg}$

(d) Velocity at point C and D,  $V_C = V_D = \sqrt{2rg}$

**(9)** Vehicle at the top of a convex over bridge,  $V_{\text{at top}} = \sqrt{rg}$

**(10)** In vertical circular motion

Total energy is constant and is T.E =  $\frac{5}{2} mgr$

**(11)** Moment of Inertia of a system of  $n$  particle.

$$I = \sum_{i=1}^n m_i r_i^2 \quad \text{or} \quad I = \int r^2 dm$$

### (12) Kinetic Energy:

(a) K.E of rigid body rotating about a given axis,

$$(K.E.)_{RM} = \frac{1}{2} I\omega^2$$

(b) K.E of rolling body.

$$\begin{aligned} (K.E)_{\text{Rolling body}} &= (K.E.)_{TM} + (K.E.)_{RM} \\ &= \frac{1}{2} mv^2 + \frac{1}{2} I\omega^2 \end{aligned}$$

(13) Radius of Gyration:  $I = MK^2$

### (14) Theorems:

(a) Parallel axes theorem,  $I_O = I_C + Mh^2$

(b) Perpendicular axes theorem,  $I_z = I_x + I_y$

### (15) Angular momentum (L):-

(a)  $\vec{L} = \vec{r} \times \vec{p}$  or  $L = r p \sin \theta$

(b)  $L = I\omega$

(16) Torque ( $\tau$ ) =  $M.I \times$  Angular acceleration

$$\tau = I\alpha$$

### (17) Body rolling down along an inclined plane:

(a) Linear speed ( $v$ ) =  $\sqrt{\frac{2gh}{1 + \frac{K^2}{R^2}}}$

where  $h$  - vertical distance (height)

(b) Linear distance ( $s$ ) =  $\frac{h}{\sin \theta}$

(c) Linear acceleration ( $a$ ) =  $\frac{g \sin \theta}{1 + \frac{K^2}{R^2}}$

**(18) Analogous Kinematical equations:**





Equation for Translational motion	Analogous Equation for Rotational motion
(1) Average velocity $v_{av} = \frac{u + v}{2}$	(1) Average angular velocity $\omega_{av} = \frac{\omega_0 + \omega}{2}$
(2) 1 <sup>st</sup> Kinematical eq <sup>n</sup> . $v = u + at$	(2) $\omega = \omega_0 + \alpha t$
(3) 2 <sup>nd</sup> Kinematical eq <sup>n</sup> $s = ut + \frac{1}{2}at^2$	(3) $\theta = \omega_0 t + \frac{1}{2} \alpha t^2$
(4) 3 <sup>rd</sup> Kinematical eq <sup>n</sup> $v^2 = u^2 + 2as$	(4) $\omega^2 = \omega_0^2 + 2 \alpha \theta$






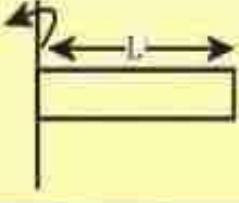
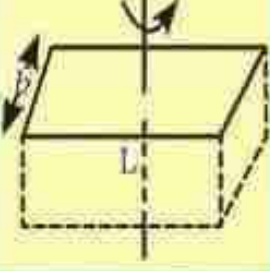
**(19) Analogous quantities between translation and rotational motion:**

Translational motion		Rotational motion		Inter relation if possible
Quantity	Expression	Quantity	Expression	
Linear displacement	$\vec{s}$	Angular displacement	$\vec{\theta}$	$\vec{s} = \vec{\theta} \times \vec{r}$
Linear velocity	$\vec{v} = \frac{d\vec{s}}{dt}$	Angular velocity	$\vec{\omega} = \frac{d\theta}{dt}$	$\vec{v} = \vec{\omega} \times \vec{r}$
Linear acceleration	$\vec{a} = \frac{d\vec{v}}{dt}$	Angular acceleration	$\vec{\alpha} = \frac{d\vec{\omega}}{dt}$	$\vec{a} = \vec{\alpha} \times \vec{r}$
Mass	$m$	Momoment of inertia	$I$	$I = \sum_{i=1}^n m_i r_i^2$ $= \int r^2 dm$

Translational motion		Rotational motion		Inter relation if possible
Quantity	Expression	Quantity	Expression	
Linear momentum	$\vec{p} = m\vec{v}$	Angular momentum	$\vec{L} = I\vec{\omega}$	$\vec{L} = \vec{r} \times \vec{p}$
Force	$\vec{f} = \frac{d\vec{p}}{dt}$	Torque	$\vec{\tau} = \frac{d\vec{L}}{dt}$	$\vec{\tau} = \vec{r} \times \vec{f}$
Work	$W = \vec{f} \cdot \vec{s}$	Work	$W = \vec{\tau} \cdot \vec{\theta}$	-
Power	$P = \frac{dW}{dt}$ $= \vec{f} \cdot \vec{v}$	Power	$P = \frac{dW}{dt} = \vec{\tau} \cdot \vec{\omega}$	-

**(20) Expression for moment of inertia for some objects:**

Object	Axis	Formula for M.I	Figure
Thin ring or hollow cylinder	Central	$I = MR^2$	
Thin ring	Diameter	$I = \frac{MR^2}{2}$	
Annular ring or thick walled hollow cylinder	Central	$I = \frac{M(r_2^2 + r_1^2)}{2}$	
Uniform disc or solid cylinder	Central	$I = \frac{1}{2}MR^2$	

Object	Axis	Formula for M.I	Figure
Uniform disc	Diameter	$I = \frac{1}{4}MR^2$	
Thin walled hollow sphere	Central	$I = \frac{2}{3}MR^2$	
Solid sphere	Central	$I = \frac{2}{5}MR^2$	
Uniform symmetric spherical shell	Central	$I = \frac{2}{5}M \frac{(r_2^5 - r_1^5)}{(r_2^3 - r_1^3)}$	
Thin uniform rod	Perpendicular to length and passing through centre	$I = \frac{ML^2}{12}$	
Thin uniform rod or rectangular plate	Perpendicular to length and about one end	$I = \frac{ML^2}{3}$	
Uniform plate or rectangular parallelopiped	Central	$I = \frac{M(L^2 + b^2)}{12}$	

Object	Axis	Formula for M.I	Figure
Uniform solid right circular cone	Central	$I = \frac{3}{10}MR^2$	
Uniform hollow right circular cone	Central	$I = \frac{MR^2}{2}$	

## Chapter 2: Mechanical Properties of Fluids

### (1) Pressure:

(a) Pressure (P) =  $\frac{\text{Force (F)}}{\text{Area (A)}}$

(b) Pressure due to liquid column

Pressure (P) =  $h\rho g$       where  $h$  = depth below free surface  
 $\rho$  = density of liquid

(c) Gauge pressure =  $P - P_0$   
=  $h\rho g$

### (2) Surface tension:

(a) Surface Tension (T)

$$T = \frac{F}{L}$$

where  $F$  = be the force acting at right angle on imaginary line - drawn on surface of liquid.

$L$  = Length of imaginary line drawn on free surface of liquid.



- (b) Surface Tension ( $T$ ) =  $\frac{W}{A}$   
where  $W$  = The surface energy of surface film  
 $A$  = Area of the film

- (c) For equilibrium of the drop

$$\cos \theta = \frac{T_2 - T_1}{T_3}$$

**(3) Excess pressure:-**

- (a) Excess pressure inside a drop

$$(P_i - P_o) = \frac{2T}{r}$$

- where  $P_i$  - Pressure inside the drop  
 $P_o$  - Pressure outside the drop  
 $r$  - Radius of drop.

- (b) Excess pressure inside a soap bubble

$$(P_i - P_o) = \frac{4T}{r}$$

**(4) Capillary rise :**

- (a) Expression for capillary rise or fall for a liquid.

$$h = \frac{2T \cos \theta}{r \rho g}$$

- (b) Surface Tension ( $T$ ),  $T = \frac{h r \rho g}{2 \cos \theta}$

- where  $h$  - rise or fall of liquid inside capillary tube  
 $\theta$  - angle of contact  
 $r$  - the radius of capillary bore  
 $\rho$  - density of liquid

- (c) Height  $\propto \frac{1}{\text{radius}}$  i.e.  $h \propto \frac{1}{r}$

**(5) Reynold's number and critical velocity of fluid:**

(a) Reynolds number ( $R_n$ ) =  $\frac{V_c \rho d}{\eta}$

(b) Critical velocity ( $V_c$ ) =  $\frac{R_n \eta}{\rho d}$

where,  $V_c$  = Critical velocity of the fluid

$R_n$  = Reynolds number

$\eta$  = Co-efficient of viscosity

$\rho$  = Density of liquid

$d$  = Diameter of tube.

**(6) Co-efficient of viscosity ( $\eta$ ):**

$$\eta = \frac{f}{A \left( \frac{dv}{dx} \right)}$$

where  $f$  = Viscous force

$A$  = Area of layer

$\frac{dv}{dx}$  = Velocity gradient

**(7) Stoke's law:-**  $F_v = 6\pi\eta r v$

**(8) Terminal velocity :**  $v = \left( \frac{2}{9} \right) \frac{r^2 g (\rho - \sigma)}{\eta}$

where -  $\rho$  - density of sphere

$\sigma$  - density of medium

$\eta$  - co-efficient of viscosity

**(9) Flux and continuity :**

(a) Mass flux =  $\rho \frac{dv}{dt} = \frac{dm}{dt}$

(b) Volume flux =  $\frac{dv}{dt}$

(c) Equation of continuity,  $A_1 V_1 = A_2 V_2$

### (10) Work done, Bernoulli's equation and Efflux

(a) Work done due to force other than conservative force of gravity

$$W = \Delta KE + \Delta PE$$

(b) Bernoulli's equation

$$(i) P_1 - P_2 = \frac{1}{2} \rho (V_2^2 - V_1^2) + \rho g (h_2 - h_1)$$

$$(ii) P + \frac{1}{2} \rho V^2 + \rho gh = \text{constant}$$

(c) Speed of efflux  $(V) = \sqrt{2gh}$

(d) Rate of flow of liquid passing through a cross section

$$2gh = V_2^2 - V_1^2$$

### Chapter 3: Kinetic theory of Gases and Radiation

#### (1) Gas Laws :

(a) Boyle's law:  $P \propto \frac{1}{V}$  i.e.  $PV = \text{constant}$  (at constant temp)

(b) Charles's law:  $V \propto T$  i.e.  $\frac{V}{T} = \text{constant}$  (at constant pressure)

(c) Gay-Lussac's law:  $P \propto T$  i.e.  $\frac{P}{T} = \text{constant}$  (at constant volume)

(d) Ideal gas equation:  $PV = nRT$

(e) Number of moles  $(n) = \frac{M}{M_0} = \frac{N}{N_A}$

(f) Boltzmann constant  $(K_B) = \frac{R}{N_A}$

#### (2) Mean free path and Rms velocity :

(a) Mean free path  $(\lambda) = \frac{1}{\sqrt{2} \pi d^2 \left(\frac{N}{V}\right)} = \frac{K_B T}{\sqrt{2} \pi d^2 \rho}$

$$(b) \text{ Mean free path } (\lambda) = \frac{AB + BC + CD + \dots}{N}$$

$$(c) \text{ Mean velocity } (\bar{C}) = \frac{C_1 + C_2 + C_3 + \dots + C_n}{N}$$

$$(d) \text{ Mean square velocity} = \frac{C_1^2 + C_2^2 + C_3^2 + \dots}{N}$$

$$(e) \text{ RMS velocity } (C) = \sqrt{\bar{C}^2} = \sqrt{\frac{C_1^2 + C_2^2 + C_3^2 + \dots}{N}}$$

**(3) The pressure exerted by gas.**

$$(a) P = \frac{1}{3} \rho c^2 \quad (b) P = \frac{1}{3} \frac{Nmc^2}{V} \quad (c) P = \frac{1}{3} \frac{M}{V} c^2$$

**(4) Rms, velocity and speed of sound :**

$$(a) \text{ RMS velocity } (C), = \sqrt{\frac{3RT}{M_0}} \quad \text{where } M_0 = N_A m \\ = \text{Molar mass of gas}$$

$$(b) C = \sqrt{\frac{3P}{\rho}}$$

$$(c) \text{ Speed of sound in a gas } (V_s) = \sqrt{\frac{\gamma RT}{M_0}}$$

where  $\gamma = \frac{C_p}{C_v}$  adiabatic constant

**(5) Kinetic Energy:**

$$(a) \text{ K.E per unit volume} = \frac{3}{2} RT$$

$$(b) \text{ K.E of one mole or one kilomole of gas} = \frac{3}{2} RT$$

$$(c) \text{ K.E per molecules} = \frac{3}{2} K.T$$

$$(d) \text{ K.E per unit mass} = \frac{3RT}{2M}$$

**(6) Mayer's relation**

**(a)**  $C_p - C_v = R$

where,  $C_p$  = Specific heat of a gas at constant pressure

$C_v$  = Specific heat of a gas at constant volume

**(b)**  $C_p - C_v = \frac{R}{J}$

where,  $J$  = Mechanical equivalent of heat

**(c)**  $S_p - S_v = \frac{R}{M_0 J}$

where,  $S_p$  and  $S_v$  = are the principal specific heats at constant pressure and volume respectively

**(7) Monoatomic, diatomic and polyatomic gases :**

**(a)** For monoatomic gases,

**(i)** Total internal energy =  $\frac{3}{2} K_B T \times N_A$

**(ii)**  $\gamma = \frac{C_p}{C_v} = \frac{5}{3}$

**(b)** For Diatomic gases:

\* For rigid gas:

**(i)** Total internal energy =  $\frac{5}{2} K_B T \times N_A$

**(ii)**  $\gamma = \frac{C_p}{C_v} = \frac{7}{5}$

\* For non rigid gas:

**(i)** Total internal energy =  $\left( \frac{5}{2} K_B T + K_B T \right) N_A$

**(ii)**  $\gamma = \frac{C_p}{C_v} = \frac{9}{7}$

**(c)** For polyatomic gases,

**(i)** Total internal energy energy =  $\left( \frac{3}{2} K_B T + \frac{3}{2} K_B T + f K_B T \right) N_A$

$$(ii) \gamma = \frac{C_p}{C_v} = \frac{4+f}{3+f}$$

**(8) Co-efficients of absorption, reflection and transmission:**

(a) Co-efficient of absorption ( $a$ ) =  $\frac{Q_a}{Q}$

(b) Co-efficient of reflection ( $r$ ) =  $\frac{Q_r}{Q}$

(c) Co-efficient of transmission ( $t$ ) =  $\frac{Q_t}{Q}$

(d)  $Q_a + Q_r + Q_t = Q$

(e)  $\therefore a + r + t = 1$

where  $Q_a$ ,  $Q_r$  &  $Q_t$  = quantity of heat absorbed, reflected & transmitted respectively.

**(9) Emissive power and Kirchhoff's law :**

(a) Emissive power ( $R$ ) =  $\frac{Q}{At}$     or     $E = \frac{Q}{At}$

(b) Coefficient of emission ( $e$ ) =  $\frac{R}{R_b}$     or     $e = \frac{E}{E_b}$

(c) Kirchhoff's law of radiation,  $a = e$

**(10) Wien's displacement law:-**

$$\lambda_{\max} = b \times \frac{1}{T} \quad \text{or} \quad \lambda_{\max} T = b$$

where  $\lambda_{\max}$  = maximum wave length

$b$  = Wien's constant

$T$  = absolute temperature

**(11) Stefan-Boltzmann Law:-**

(a)  $R = \sigma T^4$     or     $\frac{Q}{At} = \sigma T^4$

(b) For ordinary body

$$R = e\sigma T^4 \quad \text{or} \quad \frac{Q}{At} = e\sigma T^4$$

## Chapter 4: Thermodynamics

### (1) Quantity of heat and work done :

#### (a) First law of thermodynamics

$$Q = \Delta U + W$$

where  $Q$  = The quantity of heat supplied to the system.

$\Delta U$  = Increase in internal energy.

$W$  = Work done.

#### (b) Work done ( $W$ ) = $p dv$

### (2) Ideal gas equation, $pV = nRT$

### (3) First law of thermodynamics:

The first law of thermodynamics, when applied to an isothermal process,

$$Q = W = nRT \log \left( \frac{V_f}{V_i} \right)$$

### (4) Isothermal work may also be expressed as,

$$W = nRT \log \left( \frac{p_i}{p_f} \right)$$

### (5) Thermodynamics of Isobaric process

$$Q = nC_p (T_f - T_i) = nC_p \Delta T$$

### (6) Thermodynamics of Isochoric process,

$$Q = nC_v \Delta T$$

### (7) Thermodynamic of Adiabatic process

$$W = \frac{nR(T_f - T_i)}{(1 - \gamma)} = \frac{(p_f V_f - p_i V_i)}{(1 - \gamma)}$$

(8) Thermal efficiency ( $\eta$ ) of the heat engine.

$$\eta = \frac{W}{Q_H} = 1 + \frac{Q_C}{Q_H} = 1 - \frac{|Q_C|}{|Q_H|}$$

(9) Performance of a Refrigerator:-

(a) Co-efficient of performance (K) =  $\frac{|Q_C|}{W}$

(b)  $K = \frac{|Q_C|}{|Q_C| - |Q_H|}$

(10) For air conditioner:-

$$K = \frac{H}{P}$$

where, H = Rate of heat removed

P = Power required to remove heat

(11) Efficiency of a carnot cycle/engine.

$$\eta = \frac{W}{Q_H} = 1 - \frac{|Q_C|}{|Q_H|} = 1 - \frac{T_C}{T_H}$$

(12) Co-efficient of performance of a carnot refrigerator.

$$K = \frac{|Q_C|}{|Q_C| - |Q_H|} = \frac{T_C}{T_H - T_C}$$

### Chapter 5: Oscillations

(1) In linear SHM,

$$F = -kx$$

where k is force constant

(2) The differential equation of a linear SHM is

$$\frac{d^2x}{dt^2} + \frac{k}{m}x = 0 \quad \text{or} \quad \frac{d^2x}{dt^2} + \omega^2x = 0$$

where  $\omega^2 = \frac{k}{m}$  ie  $\omega = \sqrt{\frac{k}{m}}$



(3) The period of linear SHM and frequency of SHM:

$$\text{Period, } T = \frac{2\pi}{\omega} = 2\pi \sqrt{\frac{m}{k}}$$

$$\text{and Frequency } (n) = \frac{1}{2\pi} \sqrt{\frac{k}{m}}$$

(4) **Simple Harmonic motion (S.H.M.) :**

(a) Acceleration of SHM ( $a$ ) =  $-\omega^2 x$

(b) Velocity of SHM ( $v$ ) =  $\pm \omega \sqrt{A^2 - x^2}$

(c) Displacement of SHM,  $x = A \sin(\omega t + \phi)$

(5) **Extreme values of displacement, velocity and acceleration:**

At mean position	At extreme position
$x_{\min} = 0$	$x = \pm A$
$v_{\max} = \pm A\omega$	$v_{\min} = 0$
$a_{\min} = 0$	$a_{\max} = \pm \omega^2 A$

(6) **Composition of SHM:**

$$x_1 = A_1 \sin(\omega t + \phi_1)$$

$$x_2 = A_2 \sin(\omega t + \phi_2) \quad \text{are the equations of SHM}$$

(a) Equation of Resultant amplitude,

$$R = \sqrt{A_1^2 + A_2^2 + 2A_1A_2 \cos(\phi_1 - \phi_2)}$$

(b) If  $(\phi_1 - \phi_2) = 0$  then  $R = A_1 + A_2$

(c) If  $(\phi_1 - \phi_2) = \pi$  then  $R = A_1 - A_2$

(d) If  $(\phi_1 - \phi_2) = \frac{\pi}{2}$  then  $R = \sqrt{A_1^2 + A_2^2}$

(e)  $\delta = \tan^{-1} \left( \frac{A_1 \sin \phi_1 + A_2 \sin \phi_2}{A_1 \cos \phi_1 + A_2 \cos \phi_2} \right)$

**(7) Energy of particle performing SHM:**

(a) Kinetic energy,

$$E_k = \frac{1}{2} m\omega^2 A^2 \cos^2(\omega t + \phi)$$

(b) Potential energy,

$$E_p = \frac{1}{2} m\omega^2 A^2 \sin^2(\omega t + \phi)$$

(c) Total energy,

$$E = E_k + E_p = \frac{1}{2} m\omega^2 A^2$$

(d)  $E = \frac{1}{2} m(2\pi n)^2 A^2 = 2\pi^2 n^2 A^2 m$

**(8) Simple pendulum:**

(a) Period (T) =  $2\pi\sqrt{\frac{l}{g}}$

(b) Frequency (n) =  $\frac{1}{2\pi}\sqrt{\frac{g}{l}}$

(9) For seconds pendulum, T = 2sec

$$\text{length } (l) = \frac{g}{\pi^2}$$

**(10) Period of angular S.H.M.**

(a) Differential equation of angular SHM

$$\frac{d^2\theta}{dt^2} + \frac{c}{I}\theta = 0$$

(b) Period (T) =  $\frac{2\pi}{\sqrt{\text{Angular acc}^n \text{ per unit displacement}}}$

**(11) Period of magnet vibrating in uniform magnetic field:-**

$$\text{Period (T)} = 2\pi\sqrt{\frac{I}{\mu B}}$$

**(12) Damped Oscillations:**

(a) Damped force ( $F_d$ ) =  $-bv$

(b) The force on the block from the spring is

$$f_s = -kx$$

(c) Total force acting on mass at any time is

$$F = F_d + F_s$$

(d) Differential equation,  $m \frac{d^2x}{dt^2} + b \frac{dx}{dt} + Kx = 0$

(e) Angular frequency ( $\omega'$ ) =  $\sqrt{\frac{k}{m} - \left(\frac{b}{2m}\right)^2}$

(f) Period (T) =  $\frac{2\pi}{\sqrt{\frac{k}{m} - \left(\frac{b}{2m}\right)^2}}$

**Chapter 6: Superposition of Wave**

**(1) Wave motion :**

(a) Speed of wave  $v = n\lambda$

where  $n$  = Frequency of wave

$\lambda$  = Wavelength of wave

(b) Frequency ( $n$ ) =  $\frac{1}{\text{Period (T)}}$

(c) Distance covered in N vibration,  $d = N\lambda$

(d) Number of waves =  $\frac{d}{\lambda}$

(e) Phase difference in terms of distance,  $\delta = \frac{2\pi x}{\lambda}$

(f) Phase differences in terms of time,  $\delta = \frac{2\pi}{\lambda} \Delta t$

**(2) Amplitude of the Resultant wave produced due to superposition of two waves:**

$$Y_1 = A_1 \sin \omega t \text{ and } Y_2 = A_2 \sin(\omega t + \phi)$$

(a) Resultant wave  $Y = A \sin(\omega t + \phi)$

(b) Resultant amplitude is  $A = \sqrt{A_1^2 + A_2^2 + 2A_1A_2 \cos \phi}$

(c) 
$$\frac{I_{\max}}{I_{\min}} = \frac{(A_1 + A_2)^2}{(A_1 - A_2)^2}$$

**(3) Equation of stationary wave:**

$$Y = A \sin(2\pi nt) \quad \text{where } A = 2a \cos\left(\frac{2\pi x}{\lambda}\right)$$

(a) At node  $A = 0$

(b) At antinode  $A = 2a$

(c) Distance between two adjacent node or antinode  $= \frac{\lambda}{2}$

(d) Distance between adjacent antinodes and node  $= \frac{\lambda}{4}$

**(4) Vibrations of air column in a pipe:**

(a) When a pipe is closed at one end:-

(i) Fundamental frequency  $n = \frac{v}{4L}$  where  $L = l + e$

(ii) In this case only odd harmonics are present.

(b) When a pipe is open at both end:

(i) Fundamental frequency  $n = \frac{v}{2L}$  where  $L = l + 2e$

(ii) In this case all harmonics are present.

**(5) End correction (e):**

(a)  $e = 0.3d$  where  $d$  = inner diameter of pipe

(b) For pipe closed at one end,

$$e = \frac{n_1 l_1 - n_2 l_2}{2(n_2 - n_1)} = \frac{n_2 l_2 - n_1 l_1}{2(n_1 - n_2)}$$

(c) For a pipe open at both end,

$$e = \frac{n_1 l_1 - n_2 l_2}{2(n_2 - n_1)} = \frac{n_2 l_2 - n_1 l_1}{2(n_1 - n_2)}$$

### (6) Vibrations produced in a string:

(a) Speed of wave along string  $v = \sqrt{\frac{T}{m}}$

where  $T$  = Tension applied to string,

$m$  = Mass per unit length of string.

(b) Fundamental frequency ( $n$ ):-

$$n = \frac{1}{2l} \sqrt{\frac{T}{m}} \quad \text{where } l = \text{vibrating length of string}$$

(c) When string vibrates, all harmonics are present.

### (7) Laws of a vibrating string:

(a) Law of length:-  $n \propto \frac{1}{l}$       or       $nl = \text{constant}$

(b) Law of tension:-  $n \propto \sqrt{T}$       or       $\frac{n}{\sqrt{T}} = \text{constant}$

(c) Law of linear density,  $n \propto \frac{1}{\sqrt{m}}$

(d) Also  $n \propto \frac{1}{\sqrt{\rho}}$  and  $n \propto \frac{1}{r}$

### (8) Beats:

(a) Resultant eq<sup>n</sup>  $y = A \sin(2\pi n t)$

(b) Period of beat ( $T$ ) =  $\frac{1}{n_1 - n_2}$

(c) Frequency of beat ( $n$ ) =  $n_1 - n_2$

## Chapter 7: Wave Optics

### (1) Refractive index of medium with respect to air is

(a)  ${}^a\mu_m = \frac{\sin i}{\sin r}$       (b)  ${}^a\mu_m = \frac{V_a}{V_m}$       (c)  ${}^a\mu_m = \frac{\lambda_a}{\lambda_m}$

(d) Refractive index of glass *w.r.* to water,  ${}^w\mu_g = \frac{\mu_g}{\mu_w}$

### (2) Wave number and Critical angle:

(a) Wave number  $(\vec{\nu}) = \frac{1}{\lambda}$

(b) Number of wave in path  $d = \frac{d}{\lambda}$

(c) Critical angle,  $\sin c = \frac{1}{\mu}$

(d) Intensity  $\propto$  (amplitude)<sup>2</sup>

### (3) Wave vector and electric field:

(a) Wave vector  $(K) = \frac{2\pi}{\lambda}$

(b) The magnitude of electric field

$$E = E_0 \sin (Kx - \omega t)$$

where  $E_0$  = amplitude of wave

$K$  = Wave vector

### (4) Brewster's law:

(a)  $\mu_2 = \tan p$       or       $\tan p = \frac{\mu_2}{\mu_1}$

(b)  $r + p = 90^\circ$

### (5) Conditions :

(a) Condition for bright point or constructive interference path difference (P.D.) =  $n\lambda$ .

i.e P.D is equal to even multiple of  $\frac{\lambda}{2}$

(b) Condition for dark point or destructive interference path difference (P.D) =  $(2n - 1) \frac{\lambda}{2}$

i.e P.D is equal to odd multiple of  $\frac{\lambda}{2}$

(c) Path difference (P.D) =  $S_2P - S_1P$

(d) Path difference (P.D) =  $\frac{yd}{D}$

(e) Equation for  $n^{\text{th}}$  bright band  $y_n = \frac{Dn\lambda}{d}$

(f) Equation for  $n^{\text{th}}$  dark band  $y_n = \frac{D(2n - 1)\lambda}{2d}$

(6) **Fringe width (W):**

$$W = \frac{\lambda D}{d}$$

(7) Optical path =  $\mu \times d_{\text{med}}$

(8) Path difference =  $d(\mu - 1)$

(9) **Maxima and minima :**

(a) Equation of  $n^{\text{th}}$  minima,  $\sin \theta_n = \frac{n\lambda}{a}$

(b) Equation of  $n^{\text{th}}$  maxima,  $\sin \theta_n = \frac{(2n + 1)\lambda}{2a}$

(c) Width of the central bright band =  $\frac{2\lambda D}{a}$

(10) **Limit of resolution and Resolving power.**

(a) **For microscope:**

(i) Limit of resolution =  $\frac{\lambda}{2\mu \sin \theta}$

(ii) Resolving power =  $\frac{2\mu \sin \theta}{\lambda} = \frac{2(\text{N.A.})}{\lambda}$

where  $\mu$  = Refractive index of medium.

$\theta$  = Semi vertical angle.

$\lambda$  = Wave length.

$\mu \sin \theta$  = N.A. = Numerical aperture

**(b) For Telescope:**

(i) Limit of resolution =  $\frac{1.22 \lambda}{D}$

(ii) Resolving power =  $\frac{D}{1.22 \lambda}$

where  $D$  = diameter of the telescope objective

$\lambda$  = wavelength.

**(11)** Resolving power =  $\frac{1}{\text{limit of resolution}}$

### Chapter 8: Electrostatics

**(1) Charge (q) :**

**(a)** Charge ( $q$ ) =  $\pm ne$  where,  $e$  = charge of electron  
=  $1.6 \times 10^{-19}$  C

**(b)**  $q = It$   $n = 1, 2, 3 \dots$

**(2)**  $\left( \begin{array}{l} \text{Number of} \\ \text{electric lines} \\ \text{of forces} \end{array} \right) = \left( \begin{array}{l} \text{Number} \\ \text{of tube of} \\ \text{forces} \end{array} \right) = \left( \begin{array}{l} \text{Number} \\ \text{of tube of} \\ \text{induction} \end{array} \right) = \frac{q}{K\epsilon_0}$

**(3) Charge density and Electric intensity**

**(a)** Electrostatic force ( $F$ ) =  $\frac{1}{4\pi\epsilon_0} \frac{q_1 q_2}{r^2}$

**(b)** Dielectric constant ( $K$ ) =  $\frac{\epsilon}{\epsilon_0} = \frac{C}{C_{\text{air}}} = \frac{F_{\text{air}}}{F_{\text{med}}}$

**(c)** Linear charge density ( $\lambda$ ) =  $\frac{q}{l}$



(d) Surface charge density ( $\sigma$ ) =  $\frac{q}{A}$

(e) Volume charge density ( $\rho$ ) =  $\frac{q}{V}$

(f) Electric Intensity ( $E$ ) =  $\frac{F}{q_0} = \frac{V}{d} = \frac{\phi}{A}$

**(4) Gauss's law and Electric intensity :**

(a) **Gauss's law** :  $\oint \sigma E \cos \theta ds = \sum_{i=1}^n q_i$

(b) Electric intensity due to charged sphere,  $E = \frac{\sigma R^2}{\epsilon_0 r^2} = \frac{q}{4\pi\epsilon_0 r^2}$

(c) Electric intensity due to an infinite long straight charged wire,

$$E = \frac{\lambda}{2\pi\epsilon_0 r}$$

(d) Electric intensity due to charged infinite plane sheet,

$$E = \frac{\sigma}{2\epsilon_0}$$

(5) Electric potential energy ( $U$ ) =  $\frac{1}{4\pi\epsilon_0} \frac{q_1 q_2}{r}$

(6) Electric potential due to point charge,  $V = \frac{q}{4\pi\epsilon_0 r}$

**(7) Relation between E and V :-**

$$E = -\frac{dv}{dx}$$

**(8) Electric potential due to an electric dipole:-**

$$V_{\text{dipole}} = \frac{1}{4\pi\epsilon_0} \frac{p \cos \theta}{r^2}$$

where  $p = q \times 2l$  = Electric dipole moment

**(9) Electrostatics potential due to a system of charge,**

$$V_{\text{system}} = \frac{1}{4\pi\epsilon_0} \sum_{i=1}^n \frac{q_i}{r_i}$$

**(10) Potential energy :**

(a) Potential Energy of two point charges,  $= U = \frac{1}{4\pi\epsilon_0} \frac{q_1 q_2}{r_{12}}$

(b) Potential energy for a system of N charges,

$$U = \frac{1}{4\pi\epsilon_0} \sum_{j < k} \frac{q_j q_k}{r_{jk}}$$

(c) Potential energy of dipole in an external field,

$$\text{Potential energy (U)} = pE (\cos \theta_0 - \cos \theta)$$

(11) Electric susceptibility  $\chi_e = \frac{P}{E}$

(12) Capacitance (C) =  $\frac{Q}{V}$

**(13) Capacitors in series and parallel :**

(a) When Capacitors in series:-

Equivalent capacitance,

$$\frac{1}{C_s} = \frac{1}{C_1} + \frac{1}{C_2} + \frac{1}{C_3} + \dots + \frac{1}{C_n}$$

(b) When Capacitors in parallel:-

Equivalent capacitance,

$$C_p = C_1 + C_2 + C_3 + \dots + C_n$$

(c) If all capacitors are equal then.

(i) For series,  $\frac{1}{C_s} = \frac{n}{C}$

(ii) For parallel,  $C_p = nC$

(iii) Relation between  $C_s$  and  $C_p$  is

$$C_p = n^2 C_s$$

(14) Capacitance of a parallel plate capacitor without dielectric.

$$C = \frac{A\epsilon_0}{d}$$

- (15) Capacitance of parallel plate capacitor with a dielectric slab between the plates,

$$C = \frac{A\epsilon_0}{\left(d - t + \frac{t}{k}\right)}$$

- (16) Displacement and conduction current :

(a) Displacement current,  $I_d = Ak\epsilon_0 \frac{dE}{dt}$

(b) Conduction current,  $I_c = \frac{dq}{dt}$

- (17) Energy stored in capacitor (U)

(a)  $V = \frac{1}{2} \frac{Q^2}{C}$       (b)  $U = \frac{1}{2} Q.V$       (c)  $U = \frac{1}{2} CV^2$

- (18) Energy per unit volume or Energy density

$$\frac{dU}{dv} = \frac{1}{2} k\epsilon_0 E^2$$

### Chapter 9: Current Electricity

(1) Ohms law:  $V = IR \therefore$  Resistance (R) =  $\frac{V}{I}$

(2) Conductance (K) =  $\frac{1}{R}$

(3) Specific resistance ( $\rho$ ) =  $\frac{RA}{l}$

(4) Conductivity ( $\sigma$ ) =  $\frac{1}{\rho} = \frac{l}{RA}$

- (5) Kirchhoff's laws:

- (a) Kirchhoffs current law:-

$$\Sigma I = 0$$

- (b) Kirchhoffs voltage law.

$$\Sigma emf + \Sigma P.D = 0$$

**(6) Wheatstone's bridge :**

**(a)** Wheatstone network condition:

$$\frac{R_1}{R_2} = \frac{R_3}{R_4} \quad \text{or} \quad \frac{P}{Q} = \frac{S}{R}$$

**(b)** In meter bridge; condition is

$$\frac{X}{R} = \frac{l_x}{l_R} \quad \therefore X = R \frac{l_x}{l_R}$$

**(c)** In Kelvins method, condition is

$$\frac{G}{R} = \frac{l_g}{l_R} \quad \therefore G = R \frac{l_g}{l_R}$$

**(7) Potentiometer :**

**(a)** Principle of potentiometer

$$V \propto l \quad \text{or} \quad \frac{V}{l} = \text{constant}$$

**(b)** Comparison of emf by potentiometer:

**(i)** Individual method,  $\frac{E_1}{E_2} = \frac{l_1}{l_2}$

**(ii)** Sum and difference method,  $\frac{E_1}{E_2} = \frac{l_1 + l_2}{l_1 - l_2}$

**(c)** Internal resistance,  $r = R \left( \frac{l_1}{l_2} - 1 \right)$

**(8) Moving coil Galvanometer (MCG)**

**(a)** Conversion of MCG into ammeter:

**(i)** Shunt (S) =  $\left( \frac{I_g}{I - I_g} \right) G$

**(ii)** Shunt (S) =  $\frac{G}{n - 1}$

**(iii)** Fraction of total current through shunt resistance,

$$\frac{I_s}{I} = \frac{G}{S + G}$$

(iv) Fraction of total current through galvanometer,

$$\frac{I_g}{I} = \frac{S}{S + G}$$

(b) Conversion of MCG into voltmeter:

(i) High resistance (X) =  $\frac{V}{I_g} - G$

(ii) High resistance (X) =  $G(n - 1)$

### Chapter 10: Magnetic fields due to electric current

(1) **Magnetic, electric and Lorentz force:**

(a) Magnetic force  $F_m = q(\vec{V} \times \vec{B}) = qVB\sin\theta$

(b) Force due to electric field,  $F_E = Eq$

(c) Lorentz force, 
$$\begin{aligned}\vec{F} &= \vec{F}_m + \vec{F}_E \\ &= q\vec{E} + q(\vec{V} \times \vec{B}) \\ &= q[\vec{E} + (\vec{V} \times \vec{B})]\end{aligned}$$

(2) **Cyclotron formula**

$$mv = qBR \quad \text{i.e. } p = qBR$$

(3) **Cyclotron Accelerator :**

(a) Period (T) =  $\frac{2\pi m}{qB}$       (b) Frequency (n) =  $\frac{qB}{2\pi m}$

(c) K.E of ions =  $\frac{1}{2}mv^2 = \frac{q^2 B^2 R^2}{2m}$

(4) **Magnetic force :**

(a) Magnetic force in terms of current I,

$$F_m = I (l \times \vec{B}) = IlB\sin\theta$$

This is force acting on straight wire.

(b) Force on arbitrarily shaped wire,

$$\vec{F}_m = I \left[ \int d\vec{l} \right] \times \vec{B}$$

(d) Force between two long parallel wires,

$$\frac{F}{l} = \frac{\mu_0 I_1 I_2}{2\pi d}$$

(9) **Magnetic field (B) :**

(a) Magnetic field produced by current in a circular arc of a wire,

$$B = \frac{\mu_0 I \theta}{4\pi r}$$

(b) Magnetic field at the centre of circle of wire,

$$B = \frac{\mu_0 I}{2r}$$

(c) Axial magnetic field produced by current in circular loop:-

$$B = \frac{\mu_0 IR^2}{2(Z^2 + R^2)^{3/2}}$$

(10) **Ampere's Law and Magnetic field of solenoid and toroid:**

(a) Ampere Law,

$$\oint \vec{B} \cdot d\vec{s} = \mu_0 I$$

(b) Magnetic field of a solenoid

$$B = \mu_0 n l \quad \text{where } n = \frac{N}{L}$$

(c) Magnetic field of a toroid,

$$B = \mu_0 n l \quad \text{where } n = \frac{N}{2\pi r}$$

(d) Magnetic field outside the solenoid and outside the toroid is zero, i.e.  $B = 0$

### Chapter 11: Magnetic Materials

(1) **Magnetic dipole moment (M) :**

(a) (Magnetic length) =  $\frac{5}{6}$  (Geometric length)

$$2l = \frac{5}{6} L$$

(b) Magnetic dipole moment (M) =  $2l m$

**(2) Torque, angular acceleration and period :**

(a) Torque acting on magnetic dipole in uniform magnetic field,

$$\tau = MB \sin \theta$$

(b) Magnetic potential energy ( $U_m$ ) =  $- MB \cos \theta$

(c) Angular acceleration =  $-\left(\frac{MB}{I}\right)\theta$

(d) Period of angular oscillations of bar magnet,

$$T = 2\pi \sqrt{\frac{I}{MB}}$$

**(3) Magnetic moment of orbiting electron:**

(a)  $M_{orb} = IA = \frac{1}{2} e v r$

(b)  $M_{orb} = \left(\frac{e}{2m}\right)L = \frac{eh}{4\pi m_e}$

(c) Gyromagnetic ratio =  $\frac{M_{orb}}{L} = \frac{e}{2m_e}$

**(4) Magnetization, magnetic intensity and magnetic susceptibility**

(a) Magnetization ( $M_z$ ) =  $\frac{\text{Net magnetic moment } (M_{net})}{\text{Volume } (V)}$

(b) Magnetic intensity ( $H$ ) =  $nl$

(c)  $B = B_0 + B_M$  and  $B = \mu_0 (H + M)$

(d) Magnetic susceptibility ( $\chi$ ) =  $\frac{M}{H}$

(e)  $B = \mu_0 (1 + \chi)H$

(f)  $B = \mu H$  and  $\mu = \mu_0(1 + \chi)$

**(5) Curies Law and Curie temperature :**

(a) Curies Law:  $M_z = C \frac{B}{T}$       (b)  $\chi = \mu_r - 1 = C \frac{\mu_0}{T}$

(c)  $\chi = \frac{C}{T - T_c}$  where,  $C$  = Curie constant  
 $T_c$  = Curie temperature

(d)  $H = \frac{B}{\mu_0} - M$

## Chapter 12: Electromagnetic Induction

### (1) Magnetic flux and Magnetic induction :

(a) Magnetic flux  $(\phi) = B A$

(b)  $\therefore$  Magnetic induction  $B = \frac{\phi}{A}$

### (2) Faraday's law:

Magnitude of induced emf is

$$e = \frac{d\phi}{dt} \quad \dots(\text{for one turn})$$

$$e = n \frac{d\phi}{dt} \quad \dots(\text{for } n \text{ turns})$$

### (3) emf and power:

(a) emf induced in the coil,

$$e = Blv$$

(b) Motional emf in a rotating bar,

$$e = \frac{1}{2} B\omega l^2$$

(c) emf induced in a secondary coil in a changing magnetic field,

$$e_0 = \frac{2\pi\theta_0}{T}$$

(d) emf induced in rotating coil in magnetic field,

$$e = e_0 \sin\omega t$$

(e) Power =  $\vec{F} \cdot \vec{V} = \frac{B^2 L^2 V^2}{R}$

### (4) Self inductance:

(a)  $\phi = LI$  OR  $L = \frac{\phi}{I}$

(b)  $e = -L \frac{dI}{dt}$   $\therefore L = \frac{|e|}{\left| \frac{dI}{dt} \right|}$

(c) Energy of circuit =  $\frac{1}{2} LI^2$

(d) Inductances of a solenoid:  $L = \mu_0 n^2 l A$

(e) Inductances in series:  $L = L_1 + L_2 + L_3 + \dots$



(f) Inductances in parallel:  $\frac{1}{L} = \frac{1}{L_1} + \frac{1}{L_2} + \frac{1}{L_3} + \dots$

(g) Energy density of magnetic field ( $u_B$ ) =  $\frac{1}{2} \frac{B^2}{\mu_0}$

**(5) Mutual Inductance:**

(a)  $\phi_S = MI_p$  or  $M = \frac{\phi_S}{I_p}$

(b)  $e_S = -M \frac{dI_p}{dt} \therefore M = \frac{|e_S|}{\left| \frac{dI_p}{dt} \right|}$

(c) Co-efficient of coupling between two circuits,

$$L \propto N^2 \quad \text{or} \quad N \propto \sqrt{L}$$

$$\therefore N_1 N_2 = \sqrt{L_1 L_2}$$

$$\therefore M = \sqrt{L_1 L_2} \quad (\text{As } K = 1)$$

**(6) For Transformer:-**

(a)  $\frac{e_s}{e_p} = \frac{N_s}{N_p} = \frac{I_p}{I_s} = K$

where K is called transformer ratio

(b) Power of transformer,  $\eta = \frac{P_{\text{out put}}}{P_{\text{input}}} \times 100$

**Chapter 13: AC Circuits**

(1) Induced emf in rotating coil placed in uniform magnetic field,

$$e = e_0 \sin \omega t$$

where  $e_0$  is the peak value of emf.

(2) The current in circuit connected to generator,

$$I = I_0 \sin (\omega t)$$

**(3) Average and Rms Values of Ac :**

(a) Average value of AC

$$e_{av} = 0.637 e_0 \quad \text{and} \quad I_{av} = 0.637 I_0$$

(b) RMS values -

$$e_{rms} = \frac{e_0}{\sqrt{2}} \quad \text{and} \quad I_{rms} = \frac{I_0}{\sqrt{2}}$$

(4) **Resistive, inductive and capacitive circuit:**

(a) For pure resistive circuit,  $I_0 = \frac{e_0}{R}$

(b) For pure inductive circuit,  $I_0 = \frac{e_0}{\omega L}$

(c) For pure capacitive circuit,  $I_0 = \frac{e_0}{\frac{1}{\omega C}}$

(d) (i) Inductive reactance  $X_L = \omega L = 2\pi fL$

(ii) Capacitive reactance  $X_C = \frac{1}{\omega C} = \frac{1}{2\pi fC}$

(5) **LCR circuit:**

(a) Impedance  $(Z) = \sqrt{R^2 + (X_L - X_C)^2}$

(b)  $Z = \frac{e_0}{I_0}$       (c)  $\tan \phi = \left( \frac{X_L - X_C}{R} \right)$

(6) **LR and CR circuit:**

(a) For LR circuit

$$Z = \sqrt{R^2 + X_L^2}$$

(b) For CR circuit  $Z = \sqrt{R^2 + X_C^2}$

(7) **Average power and power factor:**

(a) Average power in AC circuit with resistance

$$P_{av} = e_{rms} \times I_{rms}$$

(b) Average power in AC circuit with inductor

$$P_{av} = 0$$

(c) Average power in AC circuit with capacitor

$$P_{av} = 0$$

(d) Average power in LCR circuit

$$P_{av} = e_{rms} \times I_{rms} \times \cos \phi$$

(e) Power factor  $(\cos \phi) = \frac{R}{Z} = \frac{\text{True power}}{\text{Apparent power}}$

**(8) Resonant frequency and power factor :**

(a) Resonant frequency ( $f_r$ ) =  $\frac{1}{2\pi\sqrt{LC}}$

**(b) Sharpness of Resonance:**

$$Q \text{ factor} = \frac{\omega_r}{\omega_2 - \omega_1} = \frac{\omega_r}{2 \Delta \omega} = \frac{\text{Resonant frequency}}{\text{Band width}}$$

**(c) For choke coil:**

(i) Power factor ( $\cos \phi$ ) =  $\frac{R}{\sqrt{R^2 + X_L^2}}$

(ii) Average power =  $I_{rms} \times e_{rms} \times \cos \phi$

**Chapter 14: Dual Nature of Radiation and Matter**

(1) Photon energy =  $h\nu = \frac{hc}{\lambda}$

(2) Photo electric work function ( $\phi_0$ ) =  $h\nu_0$

where  $h$  - Planck's constant

$\nu_0$  - Threshold frequency

$\nu$  - Frequency of radiation

(3) Threshold frequency ( $\nu_0$ ) =  $\frac{c}{\lambda_0}$

**(4) Einstein photo electric equation:**

$$\begin{aligned} \frac{1}{2}mv_{max}^2 &= h\nu - \phi_0 \\ &= h\nu - h\nu_0 \end{aligned}$$

**(5) Stopping potential ( $V_s$ )**

$$eV_s = \frac{1}{2}mv_{max}^2$$

**(6) De - Broglie Hypothesis:**

(a)  $p = \frac{E}{c}$  where,  $p$  - momentum

$E$  - energy of photon

(b)  $p = \frac{h}{\lambda}$   $c$  - velocity of radiation

(c)  $p = mc$

$$(d) \lambda = \frac{h}{\sqrt{2mE_k}} = \frac{h}{\sqrt{2meV}} = \frac{1.228}{\sqrt{V}} \text{ (in nm)}$$

### Chapter 15: Structure of Atoms and Nuclei

#### (1) Bohr's postulates:

(a) First postulate,  $\frac{mv^2}{r} = \frac{1}{4\pi\epsilon_0} \frac{e^2}{r^2}$

(b) Second postulate,  $mvr = \frac{nh}{2\pi}$

(c) Third postulate,  $h\nu = E_n - E_p$

#### (2) Radius of $n^{\text{th}}$ orbit,

$$r_n = \frac{n^2 h^2 \epsilon_0}{\pi m_e Z e^2}$$

(3) Velocity ( $v$ ) =  $\frac{Ze^2}{2\epsilon_0 nh}$

#### (4) Energy of an electron:

For  $n^{\text{th}}$  orbit  $E_n = -\frac{m_e Z^2 e^4}{8 \epsilon_0 n^2 h^2}$

For hydrogen atom  $Z = 1$

$$\therefore E_n = -\frac{m_e e^4}{8 \epsilon_0 n^2 h^2}$$

#### (5) Rydberg's formula:

$$\frac{1}{\lambda} = R Z^2 \left( \frac{1}{n^2} - \frac{1}{m^2} \right) \quad \text{Where R is Rydberg constant}$$

For hydrogen atom  $Z = 1$

$$\frac{1}{\lambda} = R \left( \frac{1}{n^2} - \frac{1}{m^2} \right)$$

#### (6) Five series:

(a) Lyman series  $n = 1, \quad m = 2, 3, 4, \dots \infty$

(b) Balmer series  $n = 2, \quad m = 3, 4, 5, 6 \dots \infty$

- (c) Paschen series  $n = 3, m = 4, 5, 6, \dots, \infty$   
 (d) Brachett series  $n = 4, m = 5, 6, 7, \dots, \infty$   
 (e) Pfund series  $n = 5, m = 6, 7, 8, \dots, \infty$

**(7) Debroglie hypothesis:**

(a)  $\lambda_n = \frac{2\pi r_n}{n}$       (b)  $\lambda = \frac{h}{p}$       (c)  $L_n = P_n r_n = \frac{nh}{2\pi}$

(8) Mass number (A) = Z + N

**(9) Size of nucleus:**

(a) Radius of nucleus X, is

$$R_x = R_0 A^{1/3}$$

(b) Density inside nucleus  $\rho = \frac{3mA}{4\pi R_x^3}$

**(10) Mass defect ( $\Delta m$ ):**

$$\Delta m = Zm_p + Nm_n - M$$

**(11) Binding energy:**

(a) Binding energy ( $E_B$ ) =  $\Delta m c^2$   
 $= (Zm_p + Nm_n - M)c^2$

(b) B.E per nucleon =  $\frac{B.E}{A}$

(12) Q - value = K.E =  $[m_x - m_y - m_{He}]c^2$

**(13) Law of Radioactive decay:**

(a)  $\frac{dN}{dt} = -\lambda N$       (b)  $N_{(t)} = N_0 e^{-\lambda t}$       (c)  $A_{(t)} = A_0 e^{-\lambda t}$

(d) Half life period (T) =  $\frac{0.693}{\lambda}$       (e) Average life ( $\tau$ ) =  $\frac{1}{\lambda}$

**(14) Energy released in the nuclear reaction:-**

$$Q = [m_u - m_i - m_y - 2m_n]c^2$$

(1)  $V = IR$

(2) Power (P) = VI

(3) Output voltage,  $V_o = I_L R_L$

(4)  $I_E = I_C + I_B$

(5)  $\alpha_{DC} = \frac{I_C}{I_E}$       and       $\beta_{DC} = \frac{I_C}{I_B}$

(6)  $\alpha_{DC} = \frac{\beta}{\beta + 1}$       and       $\beta_{DC} = \frac{\alpha}{\alpha - 1}$

**(7) Current and voltage gain:**

(a) Current gain ( $A_i$ ) =  $\frac{\Delta I_C}{\Delta I_B}$

(b) Voltage gain ( $A_v$ ) =  $\frac{\Delta V_o}{\Delta V_i}$

**(8) Input and output resistance:**

(a) Dynamic input resistance

$$r_i = \frac{\Delta V_{BE}}{\Delta I_B}$$

(b) Dynamic output resistance

$$r_o = \frac{\Delta V_{CE}}{\Delta I_C}$$

## Useful Information

### (1) Fundamental constants

Quantity	Symbol	Approximate value
Acceleration of free fall (Earth's surface)	$g$	$9.81 \text{ m s}^{-2}$
Gravitational constant	$G$	$6.67 \times 10^{-11} \text{ N m}^2 \text{ kg}^{-2}$
Avogadro's constant	$N_A$	$6.02 \times 10^{23} \text{ mol}^{-1}$
Gas constant	$R$	$8.31 \text{ JK}^{-1} \text{ mol}^{-1}$
Boltzmann's constant	$k_B$	$1.38 \times 10^{-23} \text{ JK}^{-1}$
Stefan - Boltzmann constant	$\sigma$	$5.67 \times 10^{-8} \text{ W m}^{-2} \text{ K}^{-4}$
Coulomb constant	$k$	$8.99 \times 10^9 \text{ N m}^2 \text{ C}^{-2}$
Permittivity of free space	$\epsilon_0$	$8.85 \times 10^{-12} \text{ C}^2 \text{ N}^{-1} \text{ m}^{-2}$
Permeability of free space	$\mu_0$	$4\pi \times 10^{-7} \text{ T m A}^{-1}$
Speed of light in vacuum	$c$	$3.00 \times 10^8 \text{ m s}^{-1}$
Planck's constant	$h$	$6.63 \times 10^{-34} \text{ J s}$
Elementary charge	$e$	$1.60 \times 10^{-19} \text{ C}$
Electron rest mass	$m_e$	$9.110 \times 10^{-31} \text{ kg}$
Proton rest mass	$m_p$	$1.673 \times 10^{-27} \text{ kg}$
Neutron rest mass	$m_n$	$1.675 \times 10^{-27} \text{ kg}$
Unified atomic mass unit	$u$	$1.661 \times 10^{-27} \text{ kg}$
Solar constant	$S$	$1.36 \times 10^3 \text{ W m}^{-2}$
Fermi radius	$R_0$	$1.20 \times 10^{-15} \text{ m}$

## (2) Metric (SI) multipliers

Prefix	Abbreviation	Value
Peta	P	$10^{15}$
tera	T	$10^{12}$
giga	G	$10^9$
mega	M	$10^6$
kilo	k	$10^3$
hecto	h	$10^2$
deca	da	$10^1$
deci	d	$10^{-1}$
centi	c	$10^{-2}$
milli	m	$10^{-3}$
micro	$\mu$	$10^{-6}$
nano	n	$10^{-9}$
pico	p	$10^{-12}$
femto	f	$10^{-15}$

## (3) Unit conversions

$$1 \text{ radian (rad)} = \frac{180^\circ}{\pi}$$

$$\text{Temperature (K)} = \text{temperature (}^\circ\text{C)} + 273$$

$$1 \text{ light year (ly)} = 9.46 \times 10^{15} \text{ m}$$

$$1 \text{ parsec (pc)} = 3.26 \text{ ly}$$

$$1 \text{ astronomical unit (AU)} = 1.50 \times 10^{11} \text{ m}$$

$$1 \text{ kilowatt-hour (kWh)} = 3.60 \times 10^6 \text{ J}$$

$$hc = 1.99 \times 10^{-25} \text{ Jm} = 1.24 \times 10^{-6} \text{ eVm}$$

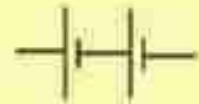


#### (4) Electrical Circuit symbols

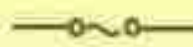
Cell



battery



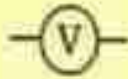
ac supply



switch



voltmeter



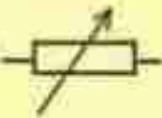
ammeter



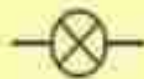
resistor



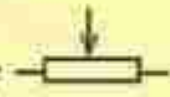
variable resistor



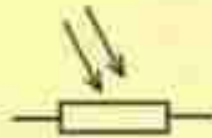
lamp



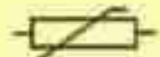
potentiometer



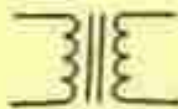
light-dependent resistor(LDR)



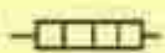
thermistor



transformer



heating element



diode



capacitor



**(5) Chemistry Notation**

Symbol	Term	Unit (s)
$c$	specific heat capacity	$J/(g \cdot ^\circ C)$ or $J/(g \cdot K)$
$E^\circ$	standard electrical potential	V or J/C
$E_k$	kinetic energy	kJ
$E_p$	potential energy	kJ
$\Delta H$	enthalpy (heat)	kJ
$\Delta H^\circ_f$	standard molar enthalpy of formation	kJ/mol
$I$	current	A or C/s
$K_c$	equilibrium constant	—
$K_a$	acid ionization (dissociation) constant	—
$K_b$	base ionization (dissociation) constant	—
$M$	molar mass	g/mol
$m$	mass	g
$n$	amount of substance	mol
$P$	pressure	kPa
$Q$	charge	C
$T$	temperature (absolute)	K
$t$	temperature (celsius)	$^\circ C$
$t$	time	s
$V$	volume	L
$C$	amount concentration	mol/L

Symbol	Term
$\Delta$	delta (change in)
$\circ$	Standard
[ ]	amount concentration

## (6) Miscellaneous

25.00 °C is equivalent to 298.15 K

Specific Heat capacities at 298.15 K and 100.000 kPa

$$\begin{aligned}
 C_{\text{air}} &= 1.01 \text{ J/(g}\cdot\text{°C)} \\
 C_{\text{polystyrene foam cup}} &= 1.01 \text{ J/(g}\cdot\text{°C)} \\
 C_{\text{copper}} &= 0.385 \text{ J/(g}\cdot\text{°C)} \\
 C_{\text{aluminium}} &= 0.897 \text{ J/(g}\cdot\text{°C)} \\
 C_{\text{iron}} &= 0.449 \text{ J/(g}\cdot\text{°C)} \\
 C_{\text{tin}} &= 0.227 \text{ J/(g}\cdot\text{°C)} \\
 C_{\text{water}} &= 4.19 \text{ J/(g}\cdot\text{°C)}
 \end{aligned}$$

**Water Autoionization Constant (Dissociation Constant)**

$$K_w = 1.0 \times 10^{-14} \text{ at } 298.15 \text{ K (for ion concentrations in mol/L)}$$

Faraday Constant

$$F = 9.665 \times 10^4 \text{ C/mol } e^-$$

Quadratic Formula

$$x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$$

## Colours of Common Aqueous Ions

Ionic species	Solution Concentration	
	1.0 mol/L	0.010 mol/L
Chromate	yellow	pale yellow
Chromium (III)	blue-green	green
Chromium (II)	dark blue	pale blue
Cobalt (II)	red	pink
Copper (I)	blue-green	pale blue-green
Copper (II)	blue	pale blue
Chromate	orange	pale orange
Nickel (II)	lime green	colourless
Nickel (III)	orange-yellow	pale yellow
Manganese (II)	pale pink	colourless
Nickel (II)	blue-green	pale blue-green